

# CerTest: enhanced performance and productivity through integration of multi-scale modelling, high-fidelity experimentation and Bayesian learning

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## 1.Challenge



New statistical frameworks must be created to design, model and test at the component level, safely accounting for uncertainty whilst exploiting new design opportunities including manufacturability.





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# Contents



1. Framework overview
2. C-spar demonstrator
3. CerTest methodology





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## 2. Process overview



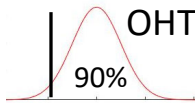
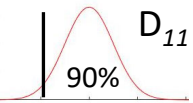
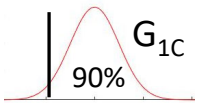
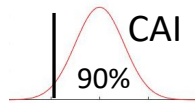
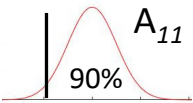
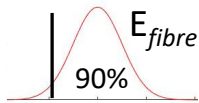
### Coupons

Material

Laminate

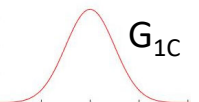
Laminate with feature

Current:



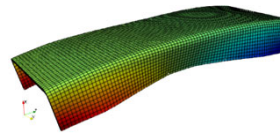
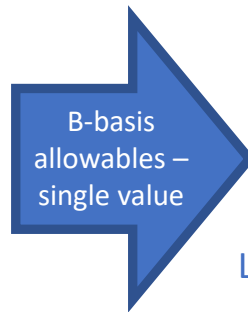
Material

CerTest:

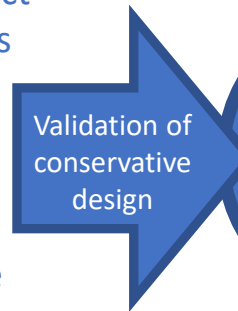


### Model/design

Models with no defect and fixed properties



Limited design space



### Test

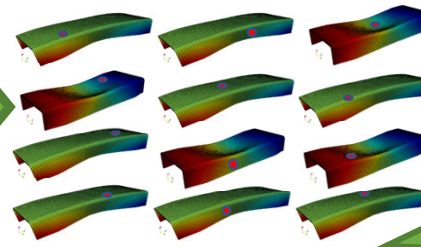
Test pyramid



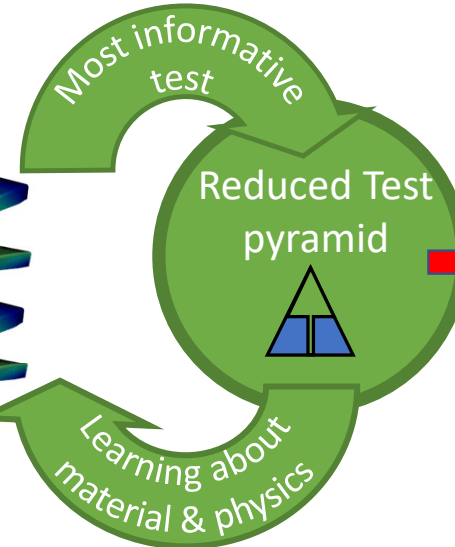
Single value  
Limit load  
pass/fail



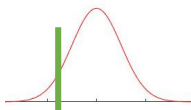
Rapid models with defects and uncertain properties



Wide design space



Reduced Test pyramid



Sufficiently probable strengths  
> limit load



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1. Overview

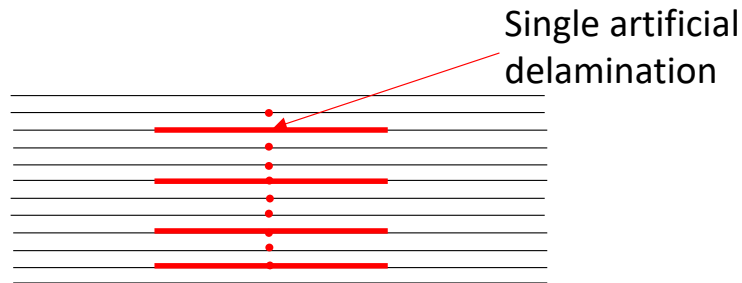
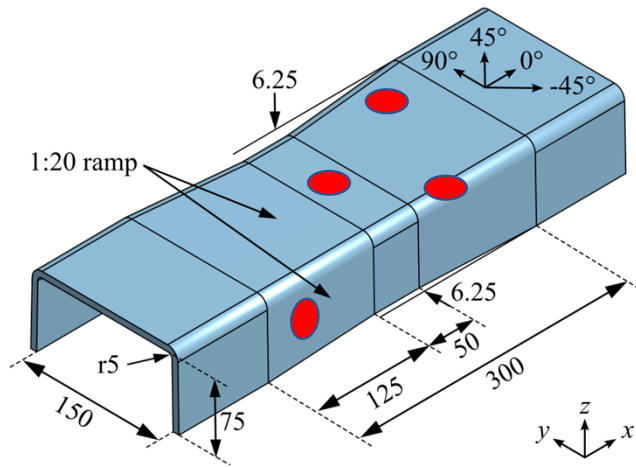
2. C-spar example description

3. CerTest methodology

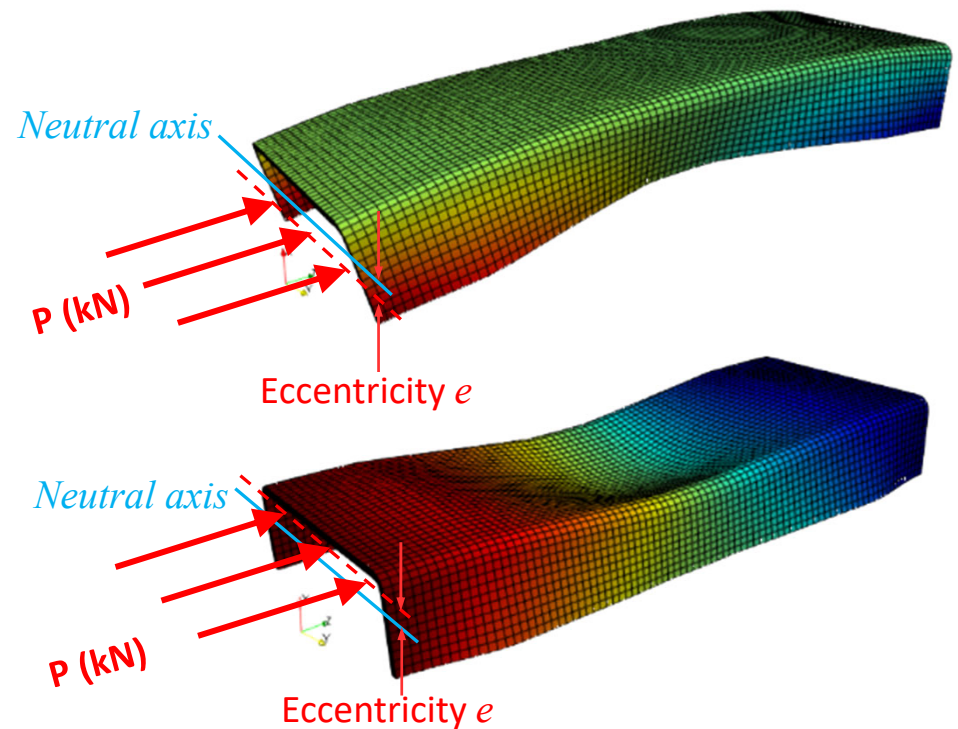


# 3. C-spar and controlled parameters

Artificial delamination position ( $d$ ): "Defect"



Eccentric loading ( $e$ ): "Load cases"



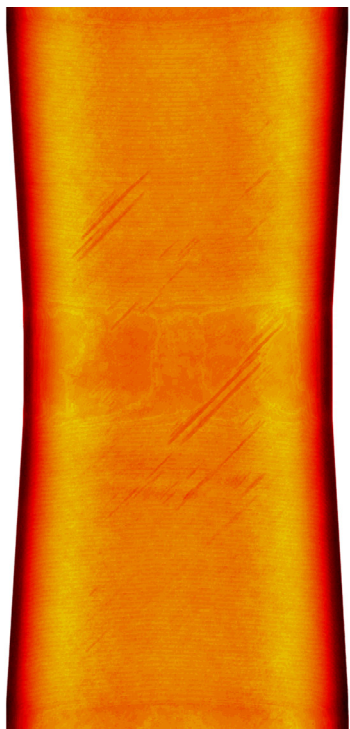


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# 4. C-spar demonstrator - data

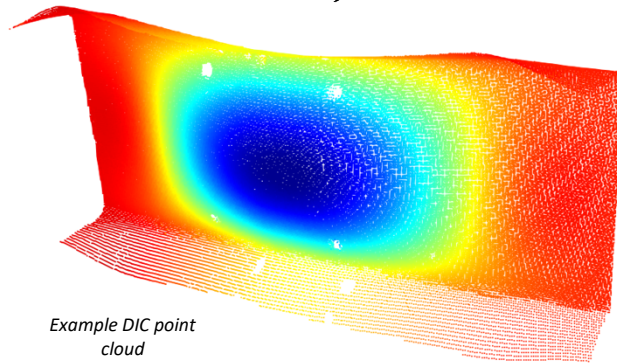


NDE: X-ray CT, CMM, Ultrasound, eddy current



Thickness (mm)  
8.0  
7.0  
6.0  
5.0  
4.0

Physical test: DIC



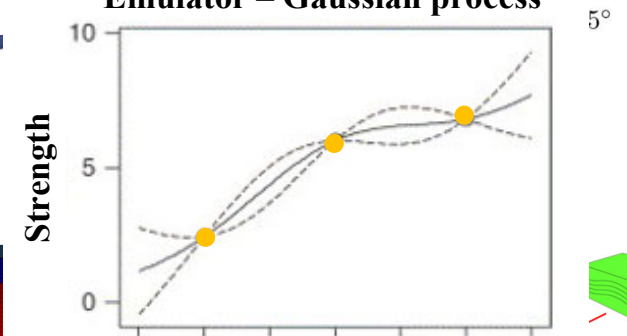
Example DIC point cloud

1.9e+00  
1  
0  
-1  
-2  
-3  
-4  
-5  
-6  
-7  
-8  
-9.5e+00

Simulation: DUNE and ABAQUS (FE<sup>2</sup>)

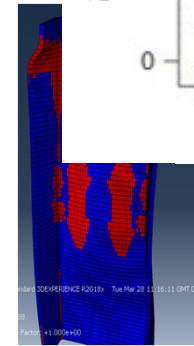
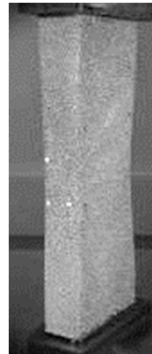
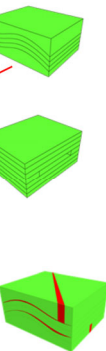


Emulator – Gaussian process



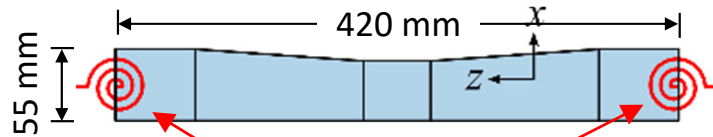
Strength

Eccentricity

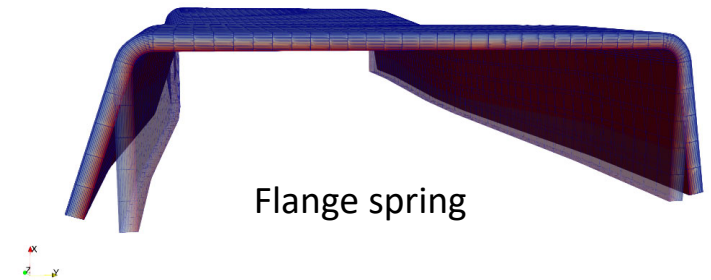




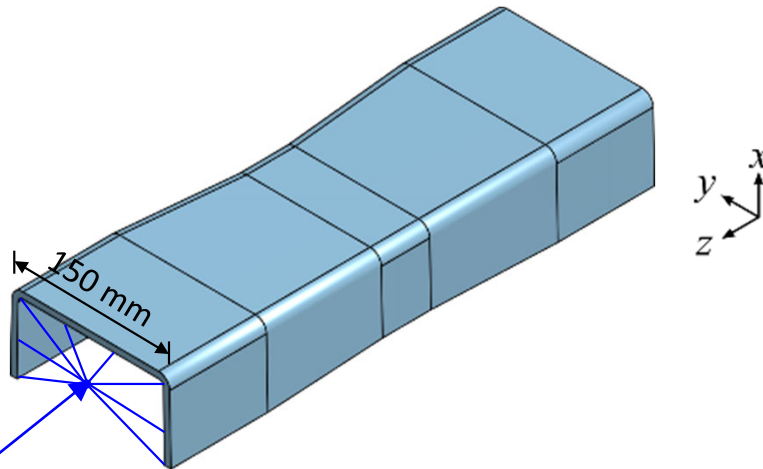
# 5. Parameter uncertainty - BCs



Torsional springs with stiffness,  $K$ , control BC strength

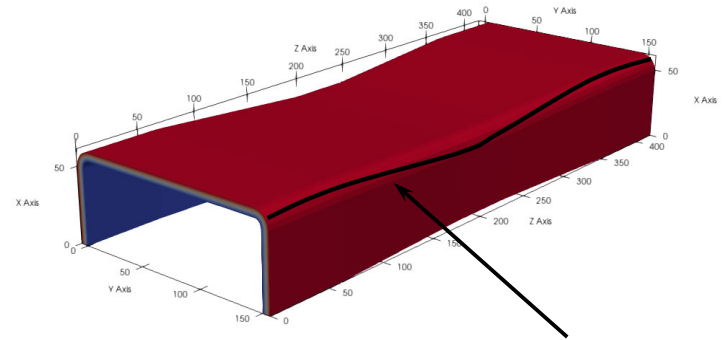


Flange spring



Ends constrained to reference points with beam MPCs

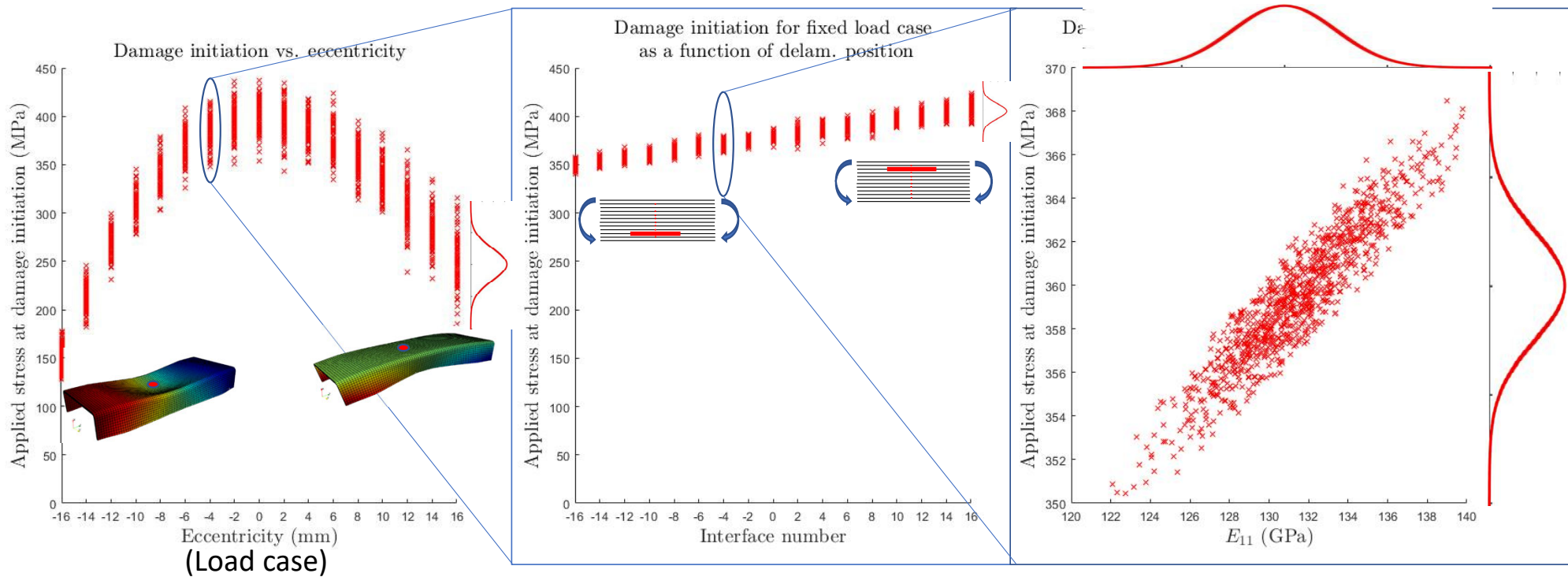
$$u_1 = u_2 = R_1 = R_3 = 0$$



Fibre path owing to conformation with geometry e.g. not straight.



# 6. Parameter uncertainty - material





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# 7. Discrepancy model

Experiment

Numerical simulation output

Discrepancy

Measurement error

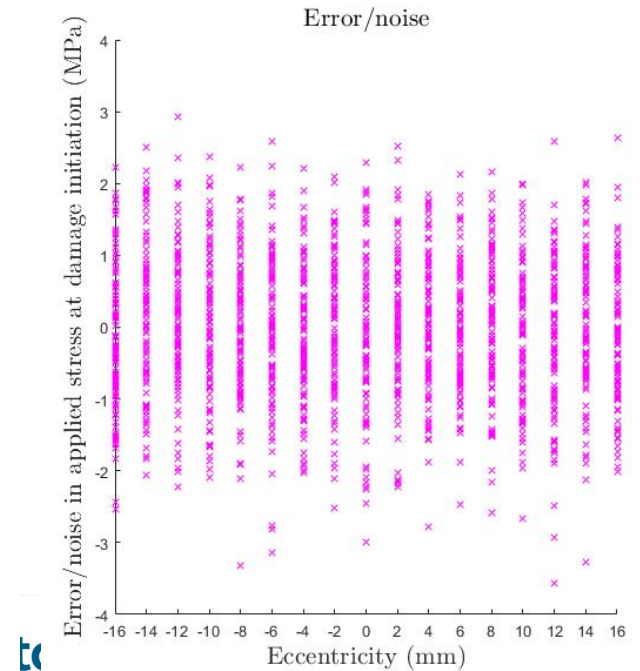
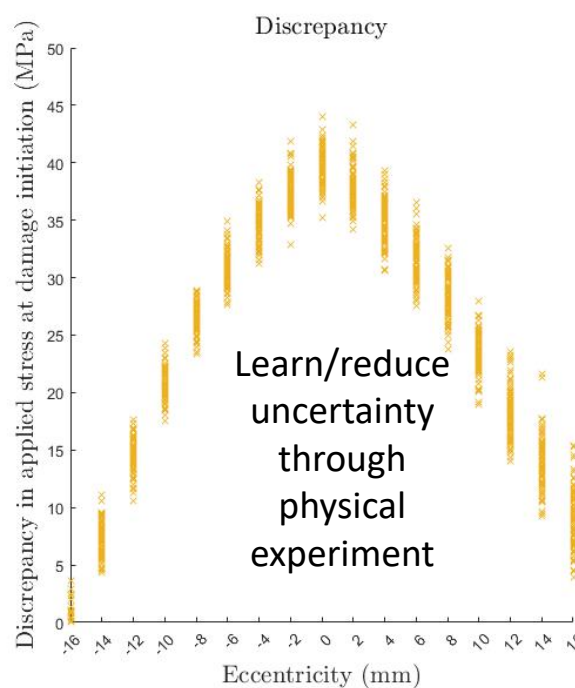
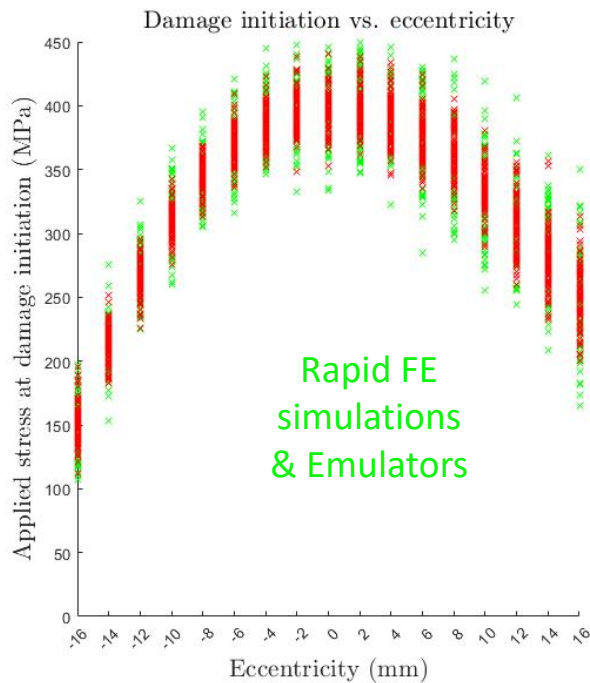
$$y(x_i, \theta^*) = \eta(x_i, \theta^*)$$

$$+ \delta(x_i, \theta^*)$$

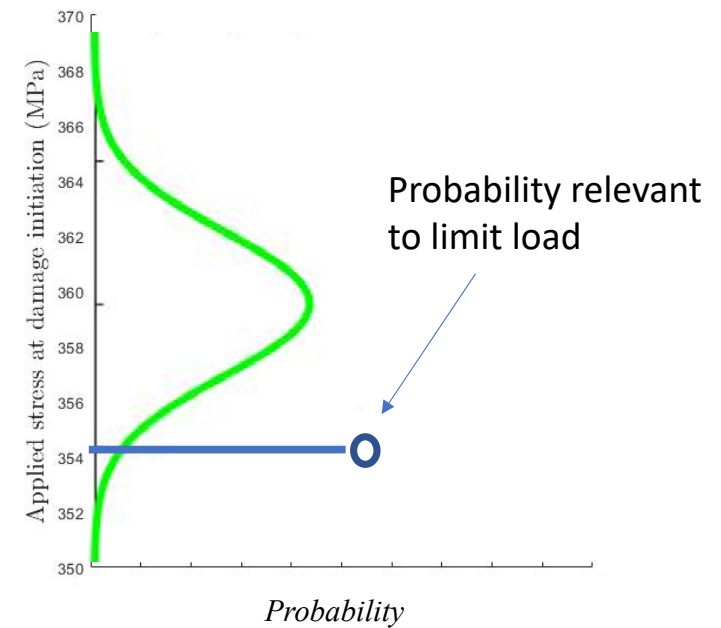
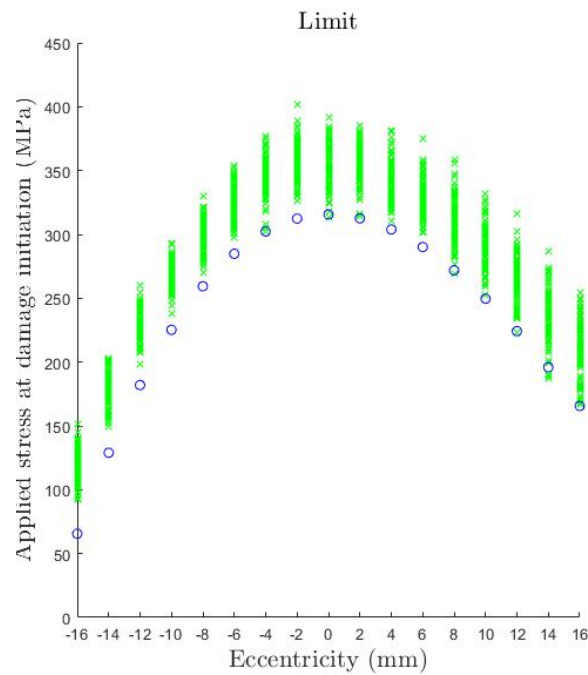
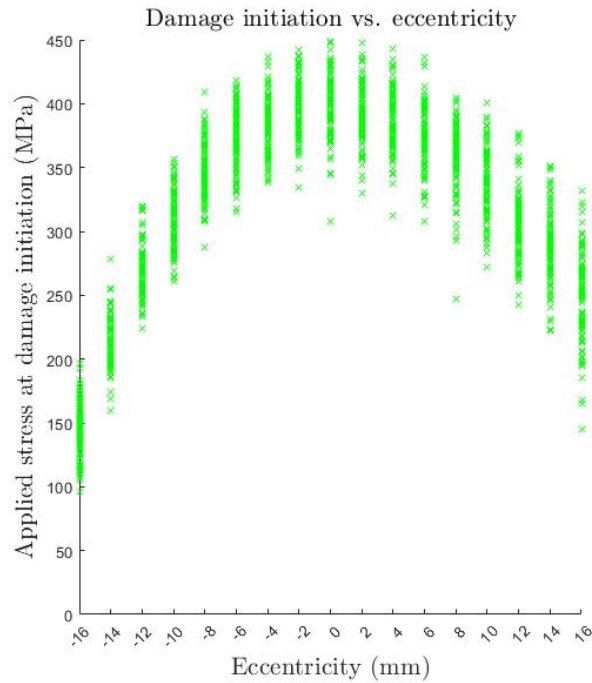
$$+ \epsilon_i$$

Controllable (delamination position and eccentricity)

Uncertain (e.g. modulus, boundary conditions)



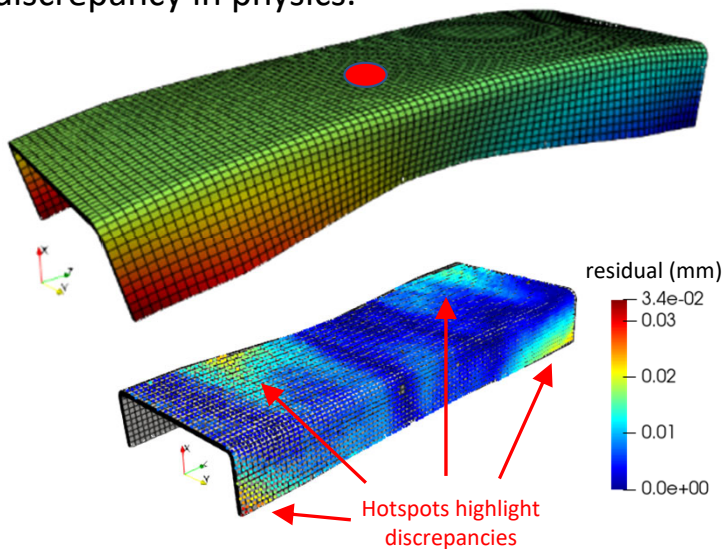
# 8. Limit load





## Single physical experiment

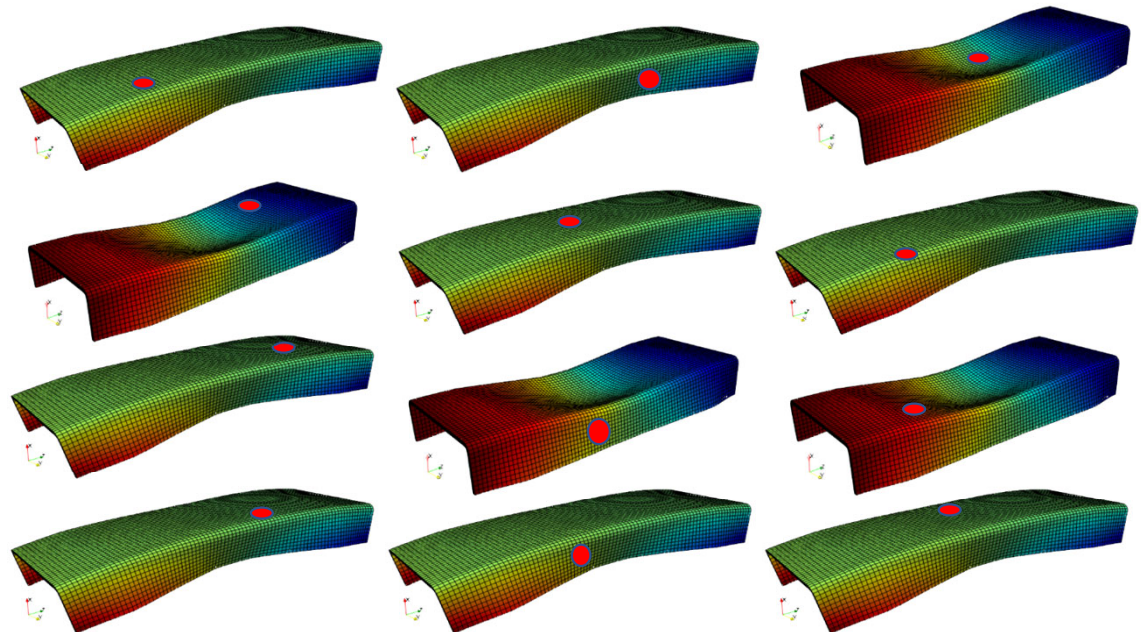
Learn about (via comparison of DIC and simulations), and then employ, property/BC values for the specific part instance to uncover discrepancy in physics.



Residuals of DIC compared with average calibrated model

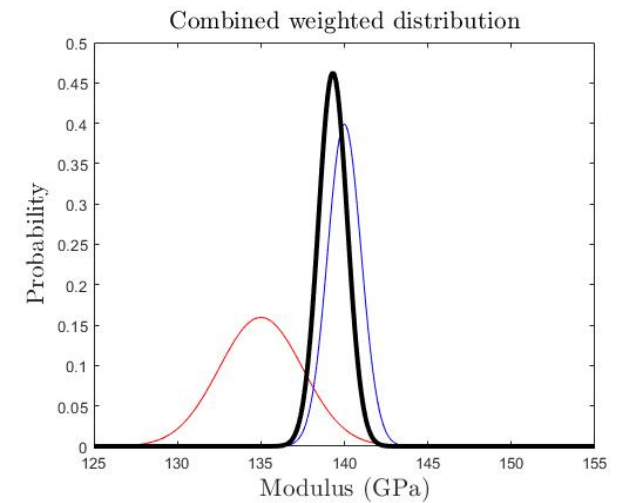
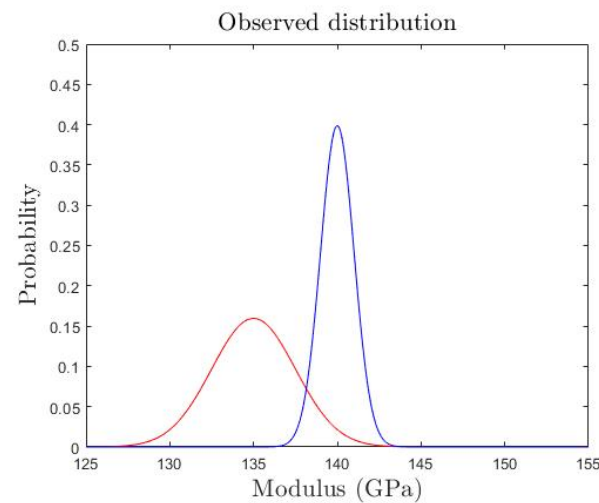
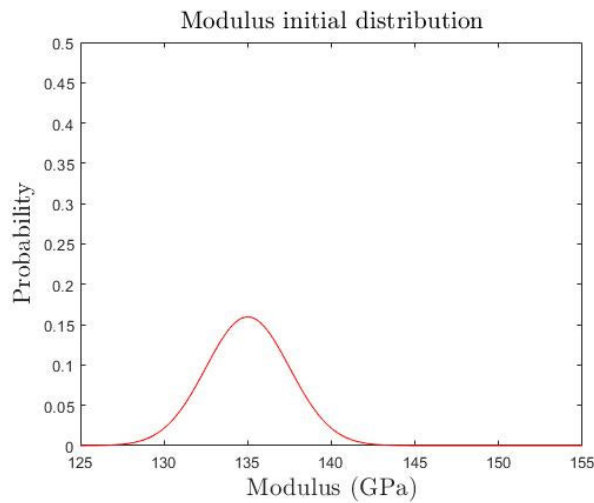
## 'All' C-spars with defect under all load cases

Choose tests to learn about and minimise discrepancy in physics as behaviour varies at the part scale.

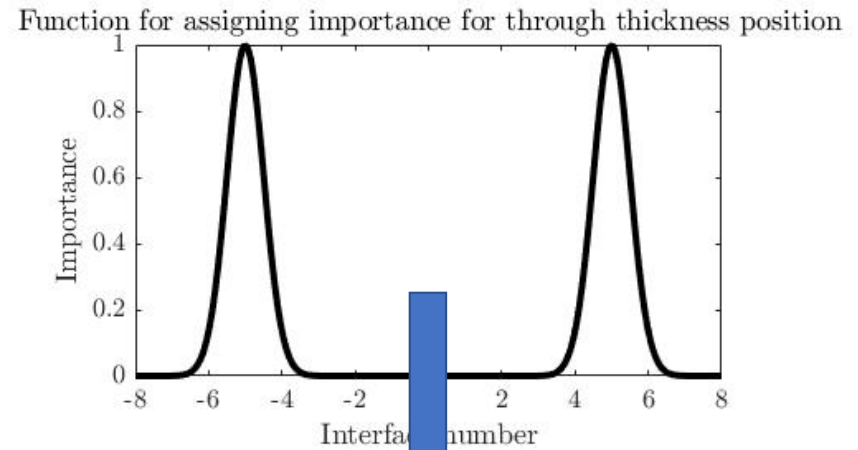
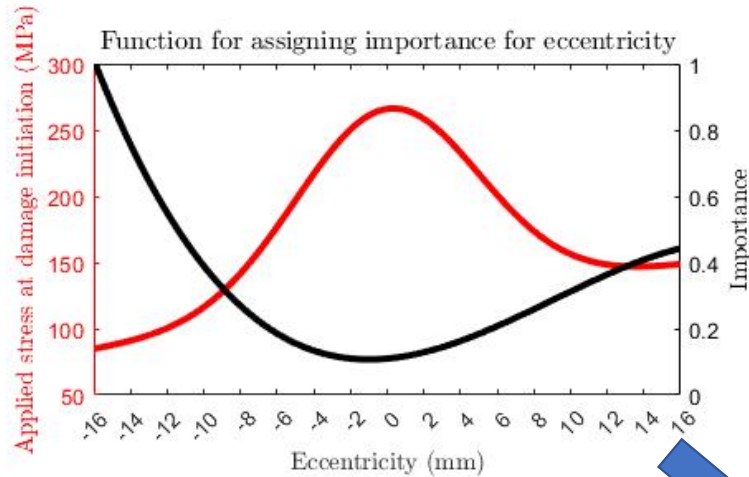


# 10. Bayesian calibration

## Single experiment

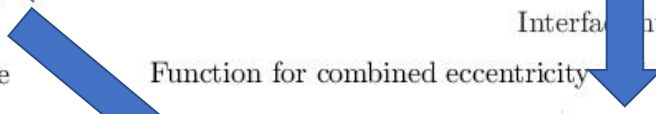
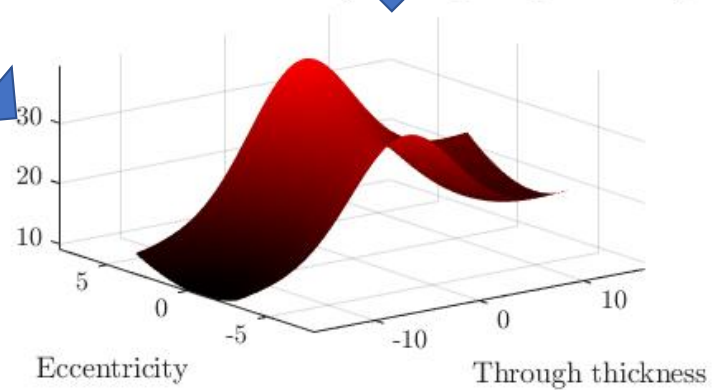
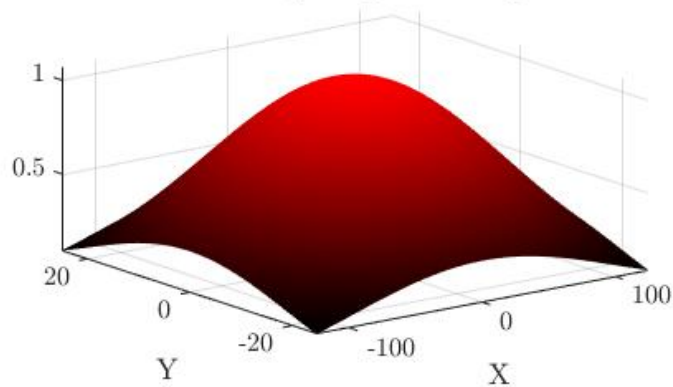


# 11. Design of experiments & Importance

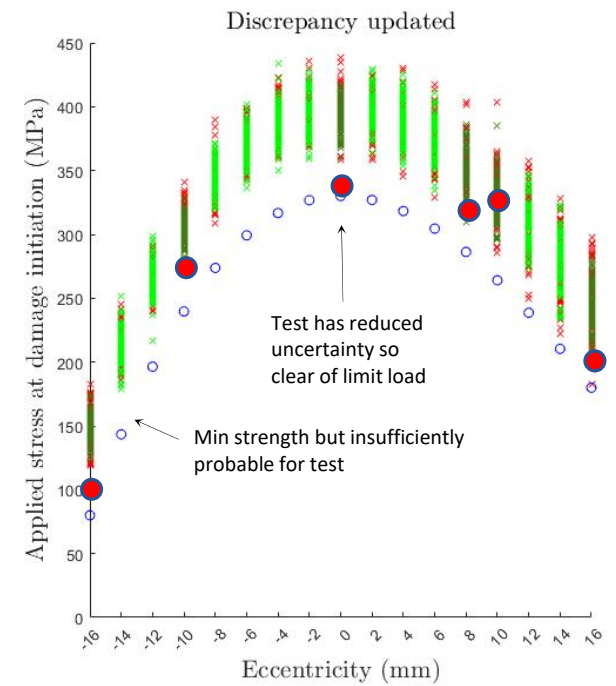
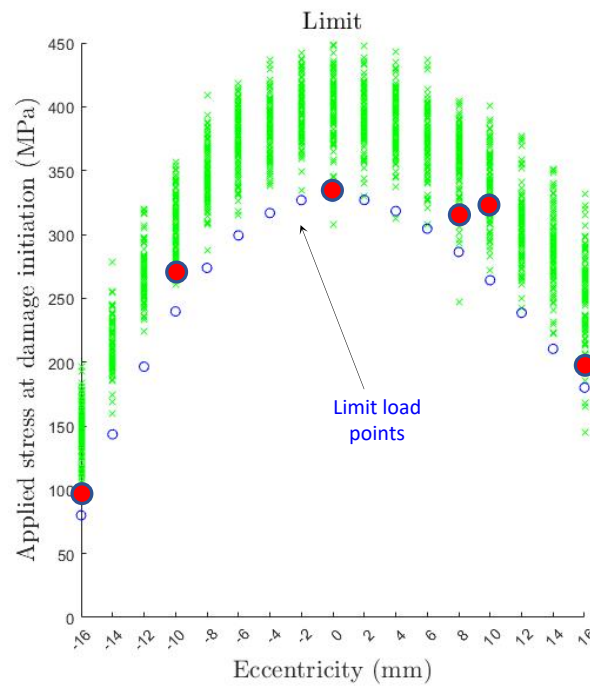
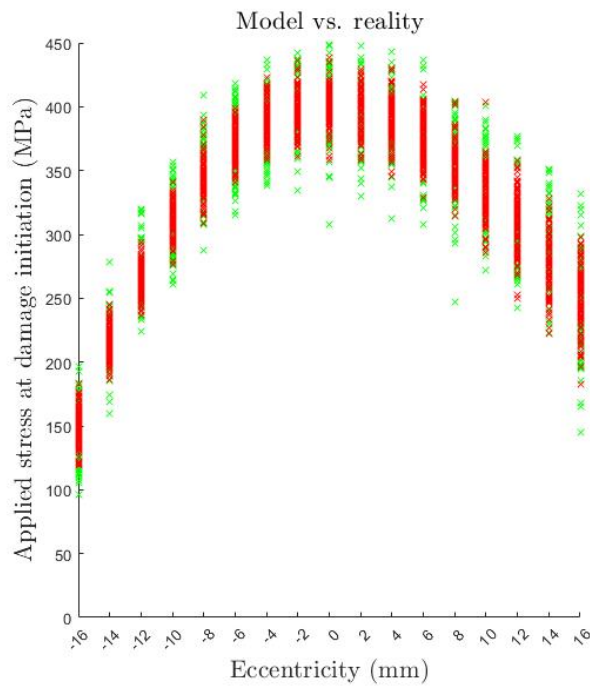


Function for in-plane position importance

Function for combined eccentricity in-plane position importance









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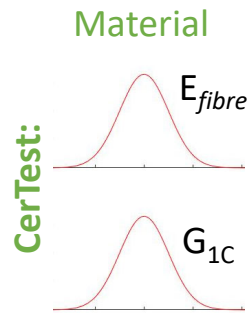
# 13. Conclusions & future work



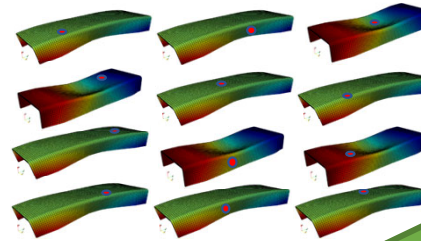
Coupons

Model/design

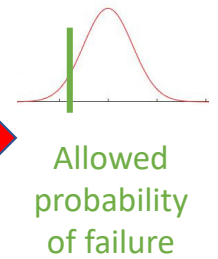
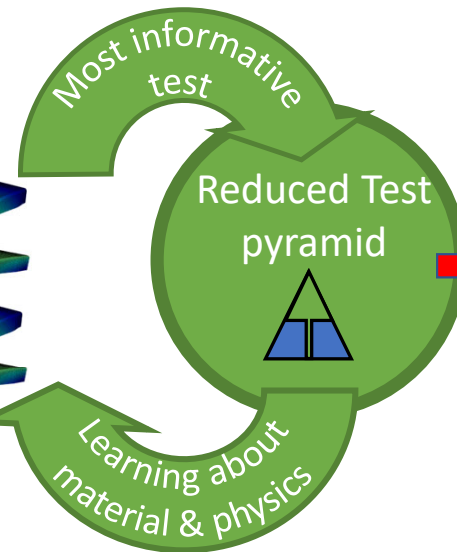
Test



Rapid models with defects and uncertain properties



Wide design space



Potential to: (a) consider material variability at scale e.g. defects and fibre steering  
 (b) Understand the impact of process variability on strength – rapid uptake of new materials





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# 14. CerTest Team



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Research Associates

PhDs

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			 <b>Riccardo Cappello</b> <a href="mailto:riccardo.Cappello@bristol.ac.uk">riccardo.Cappello@bristol.ac.uk</a>	 <b>Rafael Ruiz Iglesias</b> <a href="mailto:rafael.ruiziglesias@bristol.ac.uk">rafael.ruiziglesias@bristol.ac.uk</a>
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			 <b>Carl Scarth</b> <a href="mailto:C.Scarth@bath.ac.uk">C.Scarth@bath.ac.uk</a>	 <b>Sinan Xiao</b> <a href="mailto:Sx450@bath.ac.uk">Sx450@bath.ac.uk</a>
				 <b>Thomas Maierhofer</b> <a href="mailto:Tam48@bath.ac.uk">Tam48@bath.ac.uk</a>

Tues

Tues

Wed

Thur

Wed